

# AN ORTHOGONAL SPECTRUM SHARING SCHEME FOR COGNITIVE LTE NETWORKS

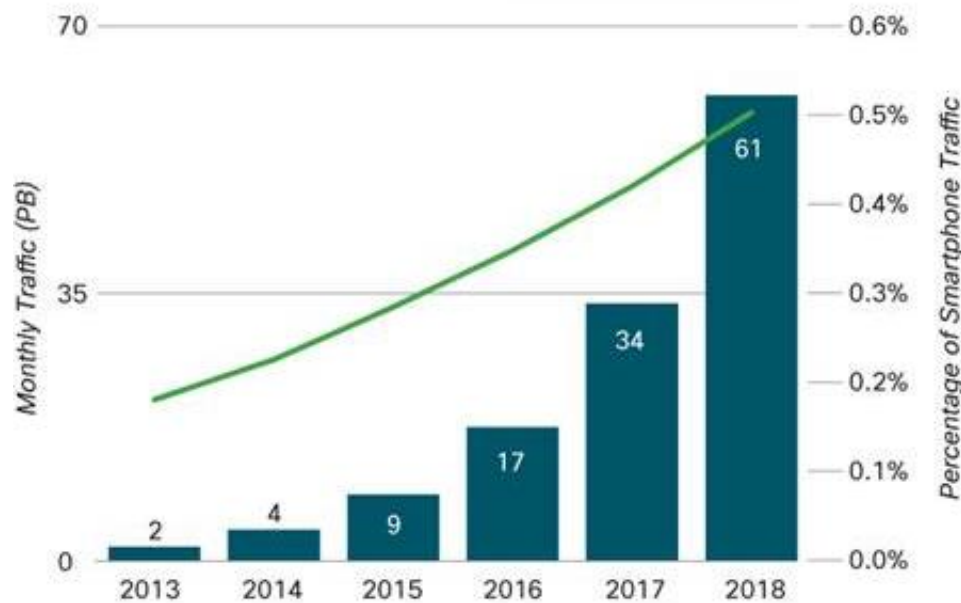
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**SDR WInnComm 2014**

# The Need for Spectrum Sharing



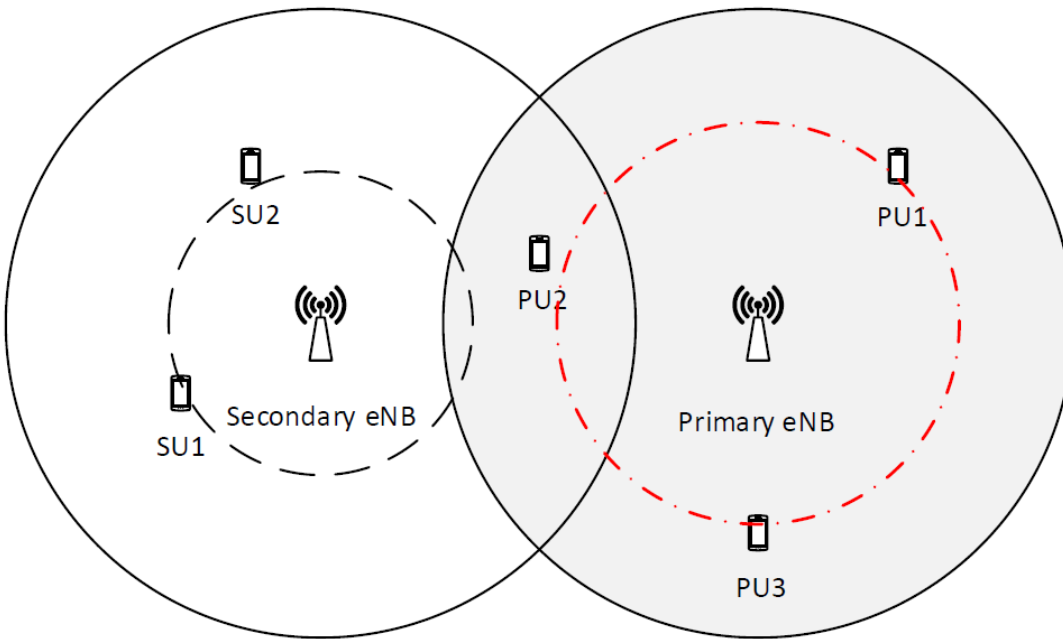
Source: Cisco VNI Mobile, 2014

- Global mobile data traffic rapidly increasing
- Need for new and innovative technologies
- Spectrum Sharing is one such promising technique
- Spectrum sharing among cellular operators is explored in this paper

# In this paper...

- Novel Framework for inter-operator spectrum sharing
  - Spectrum cost based rate maximization
  - Assumption: No frequency reuse (orthogonal scheme)
- Optimal Resource Allocation for Users
  - Problem formulation for simple framework
  - Analytical solutions and cost factor analysis
- Extension for multiuser LTE system
  - Problem formulation based on Physical Resource Blocks (PRB)
  - Numerical solution and network simulation for a LTE
- Conclusions and Future Work

# System Model (1/2)



System Model from the perspective of one operator

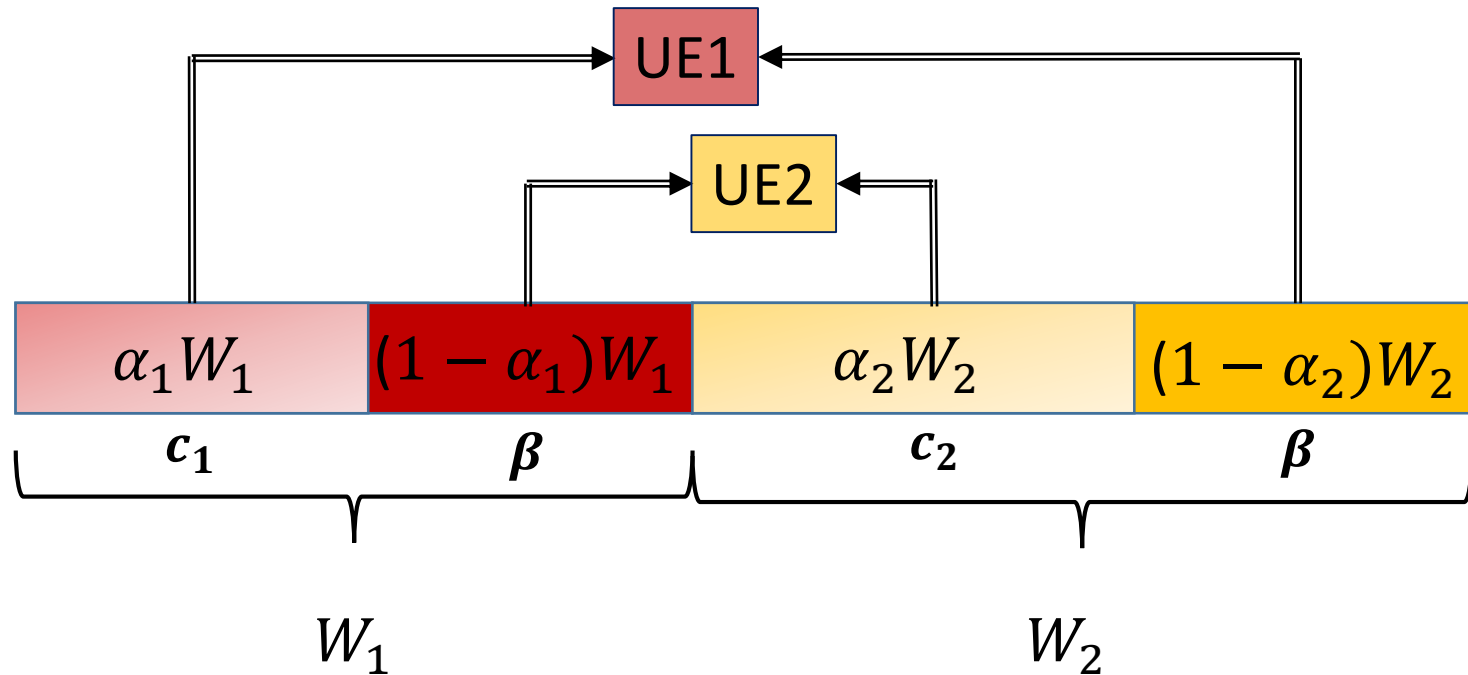
## **In our Problem...**

OP1, OP2 – Two operators

UE1, UE2 – Two Users

- Different costs to access different spectrum
- Based on the costs, resource allocations are made to users
- Minimum rate constraint to ensure fairness

# System Model (2/2)



- **Normalized Cost Metric** –  $c_i \propto \frac{1}{\text{cost incurred to allocate unit BW}}$
- $c_1, c_2$  – cost metric for accessing parent spectrum
- $\beta$  – cost metric for accessing secondary spectrum

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# The Optimization Problem

- Capacity,  $R = 1 + \log(1 + \gamma_{ij})$ ,  $\gamma_{ij}$  – SINR
- Constrained Rate Maximization

$$\max_{\alpha_1, \alpha_2} \mathcal{J} = \alpha_1 c_1 W_1 \log(1 + \gamma_{11}) + \text{—————} \rightarrow \text{UE1-OP1}$$

$$(1 - \alpha_2) \beta W_2 \log(1 + \gamma_{12}) + \text{—————} \rightarrow \text{UE1-OP2}$$

$$\alpha_2 c_2 W_2 \log(1 + \gamma_{22}) + \text{—————} \rightarrow \text{UE2-OP2}$$

$$(1 - \alpha_1) \beta W_1 \log(1 + \gamma_{21}) \text{ —————} \rightarrow \text{UE2-OP1}$$

s.t.

$$\alpha_1 c_1 W_1 \log(1 + \gamma_{11}) + (1 - \alpha_2) \beta W_2 \log(1 + \gamma_{12}) \geq R_1$$

$$\alpha_2 c_2 W_2 \log(1 + \gamma_{22}) + (1 - \alpha_1) \beta W_1 \log(1 + \gamma_{21}) \geq R_2$$

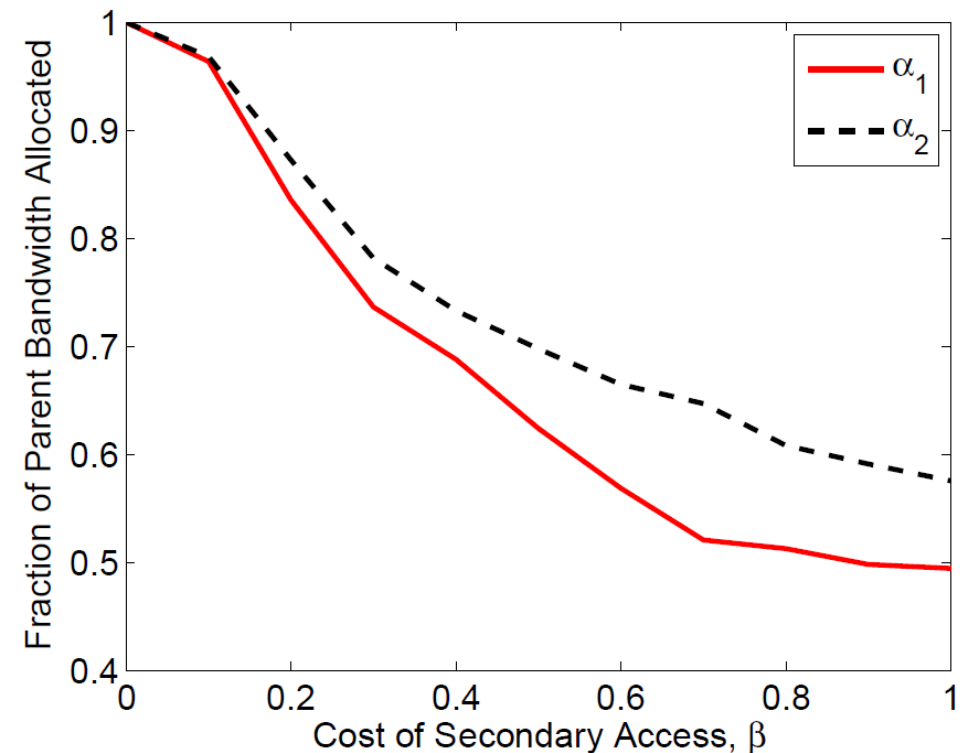
$$0 \leq \alpha_1 \leq 1$$

$$0 \leq \alpha_2 \leq 1$$

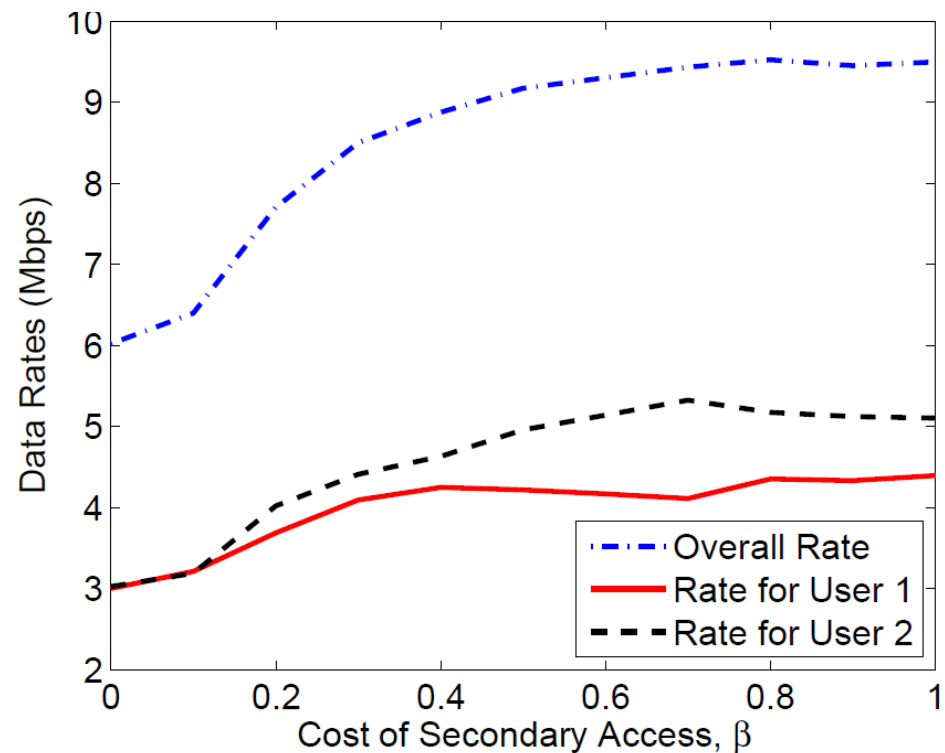
$$(\alpha_1^*, \alpha_2^*) = \psi_i \in \Psi : \arg \max_{\forall \Psi} \mathcal{J}$$

# Numerical Results (1/4)

Case 1:  $c_1 = 0.5$ ,  $c_2 = 0.7$ ,  $W_1 = W_2 = 3$  MHz.



Variation of  $\alpha$ 's with cost of secondary spectrum

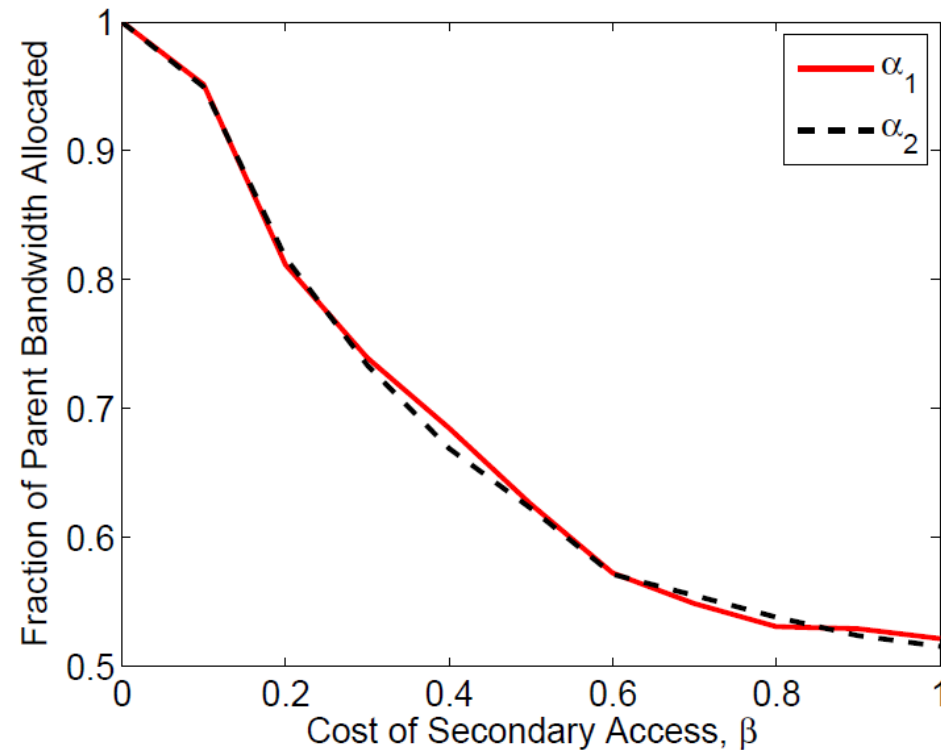


Variation of data rate with cost of secondary spectrum

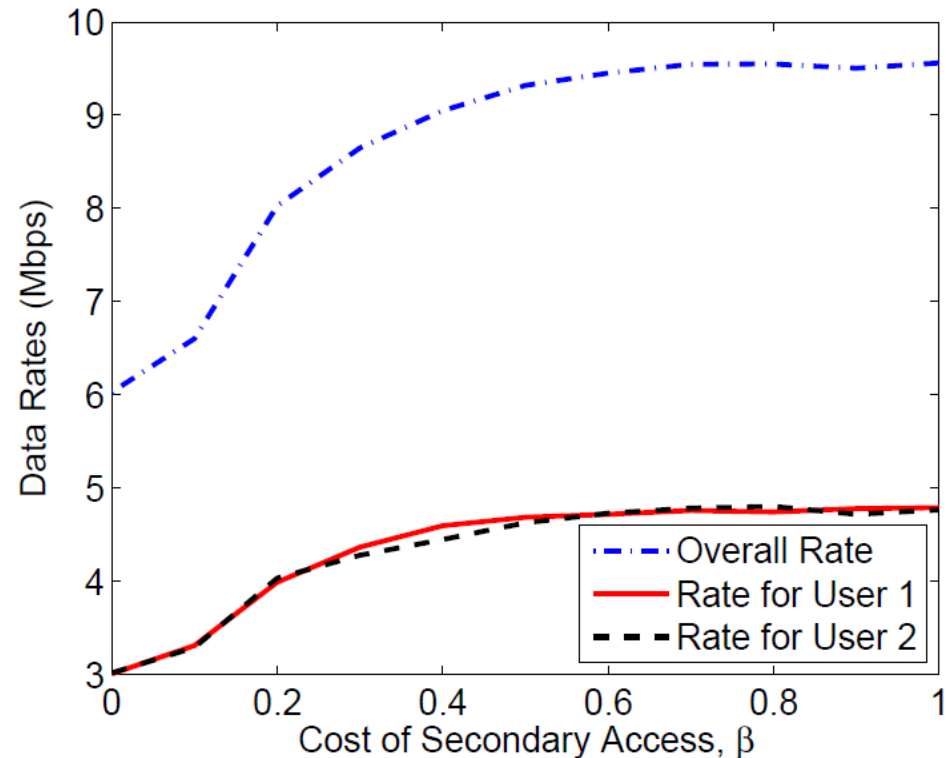


# Numerical Results (2/4)

Case 2:  $c_1 = c_2 = 0.5$ ,  $W_1 = W_2 = 3$  MHz



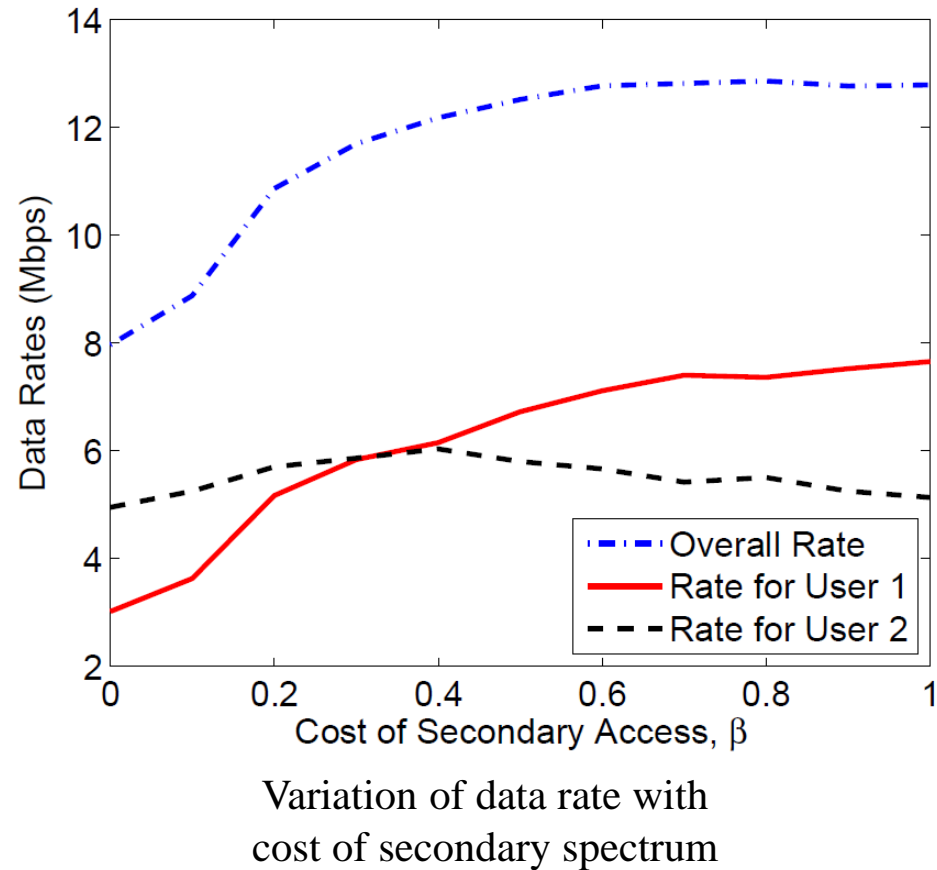
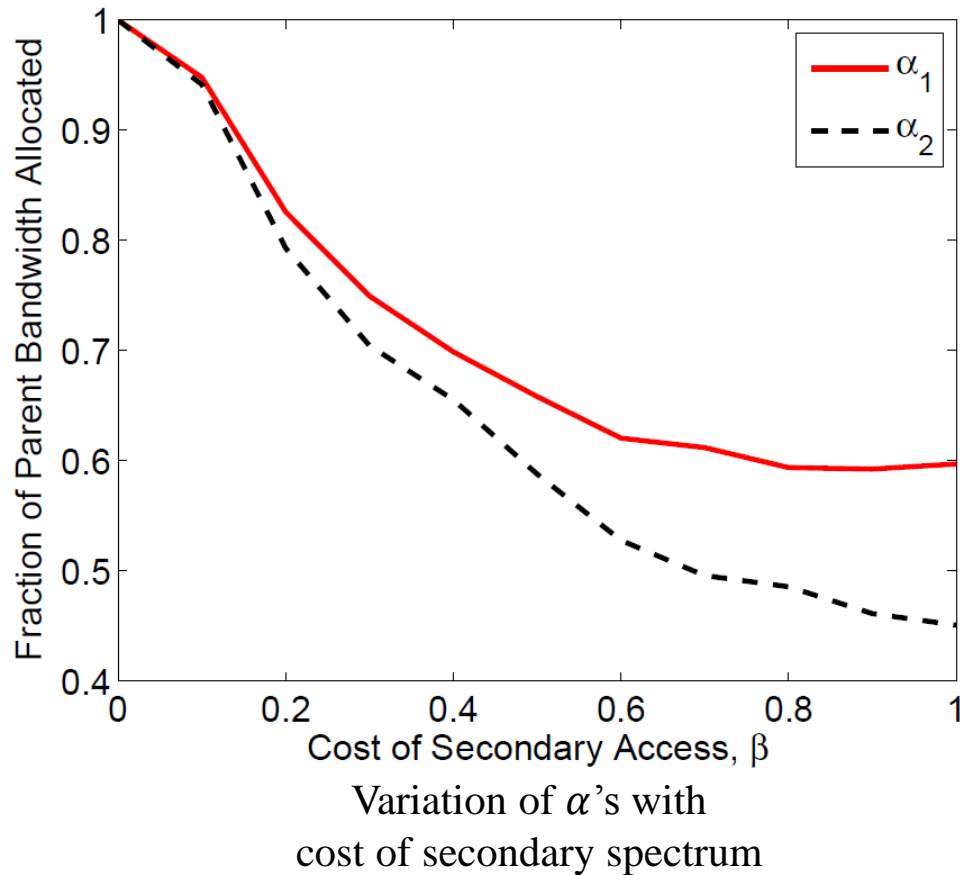
Variation of  $\alpha$ 's with cost of secondary spectrum



Variation of data rate with cost of secondary spectrum

# Numerical Results (3/4)

Case 3:  $c_1 = c_2 = 0.5$ ,  $W_1 = 3\text{MHz}$ ,  $W_2 = 5\text{ MHz}$



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# Extension to LTE Networks

- Reformulated as a PRB assignment problem
- Optimization becomes a binary integer program
- Definition of cost metric:

$$\mathcal{C}_{i,j} = c_1 \quad \forall i \in \mathbb{I}_1, j \in \mathbb{J}_1$$

$$\mathcal{C}_{i,j} = c_2 \quad \forall i \in \mathbb{I}_2, j \in \mathbb{J}_2$$

$$\mathcal{C}_{i,j} = \beta \quad \forall i \in \mathbb{I}_1, j \in \mathbb{J}_2$$

$$\mathcal{C}_{i,j} = \beta \quad \forall i \in \mathbb{I}_2, j \in \mathbb{J}_1$$

where  $\mathbb{I}_1, \mathbb{I}_2$  – Set of PRBs in OP1 and OP2's networks respectively

$\mathbb{J}_1, \mathbb{J}_2$  – Set of UEs in OP1 and OP2's networks

# Resource Scheduling for LTE (1/2)

- Binary assignment variable :

$$x_{i,j,t} = \begin{cases} 1 & \text{if } i^{\text{th}} \text{ PRB is assigned to } j^{\text{th}} \text{ UE} \\ 0 & \text{if } i^{\text{th}} \text{ PRB is } \textit{not} \text{ assigned to } j^{\text{th}} \text{ UE} \end{cases}$$

- Joint optimization problem:

$$\begin{aligned} \max_{x_{i,j,t}} \quad & \sum_{j=1}^J x_{i,j,t} C_{i,j} R_{i,j,t} \quad \text{s.t.} \quad \sum_{j=1}^J x_{i,j,t} \in \{0, 1\}, \\ & \sum_{i=1}^I (x_{i,j,t} R_{i,j,t}) > R_{j,t}^{\min}, \quad \nearrow \text{Per UE QoS guarantee} \\ & \sum_{i=1}^I (x_{i,j,t} R_{i,j,t}) < R_{j,t}^{\max}, \quad \searrow \text{Max rate per UE} \end{aligned}$$

# Resource Scheduling for LTE (2/2)

- Problem can be solved numerically
- Evaluation of spectrum assignment metrics  $\alpha_1, \alpha_2$  :

$$\alpha_1 = \frac{1}{|\mathbb{I}_1|} \cdot \sum_{j \in \mathbb{J}_1} \sum_{i \in \mathbb{I}_1} x_{i,j,t}$$

$$\alpha_2 = \frac{1}{|\mathbb{I}_2|} \cdot \sum_{j \in \mathbb{J}_2} \sum_{i \in \mathbb{I}_2} x_{i,j,t}$$

- Cost optimal spectrum allocation solution

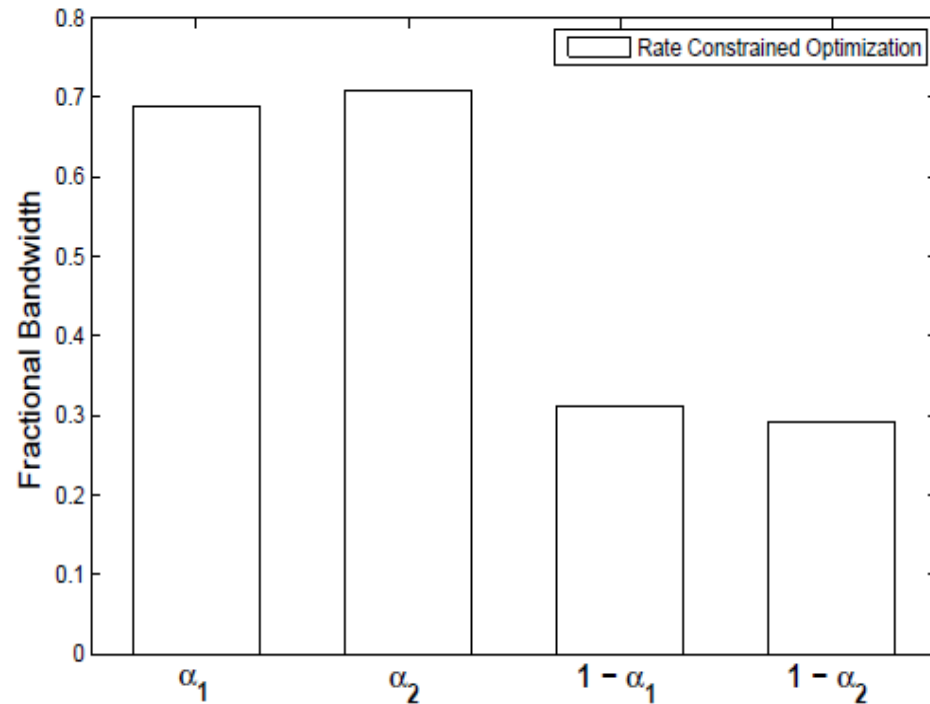
# Simulation Results (1/3)

## Simulation Parameters

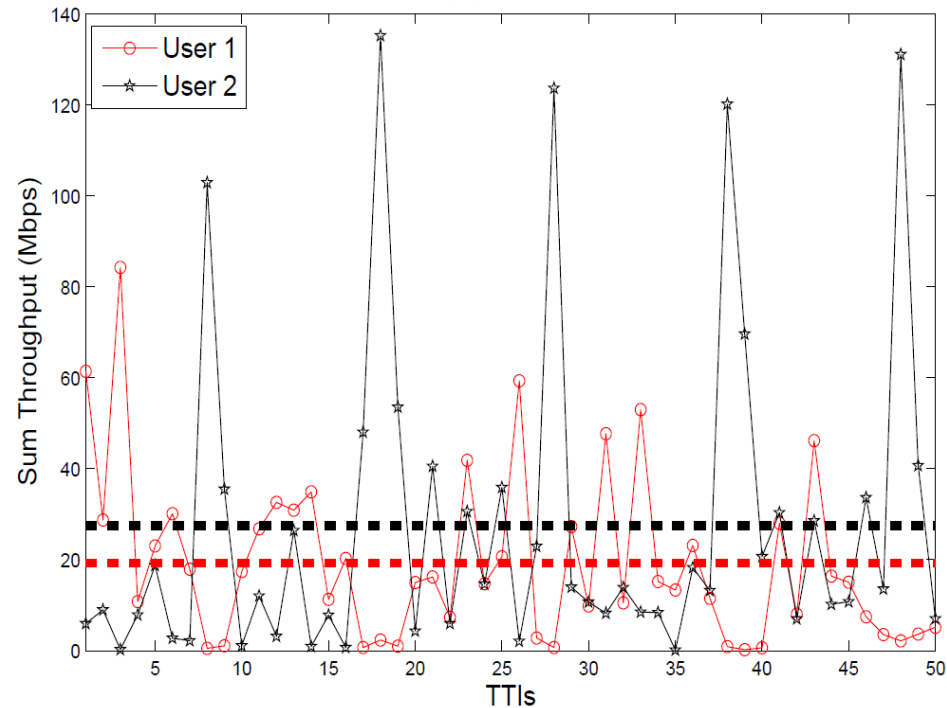
Channel Model	COST-Hata Model
Center Frequency of Operator 1	1800 MHz
Center Frequency of Operator 2	1900 MHz
Sub-carrier separation ( $\Delta f$ )	15 kHz
LTE system bandwidth (Operator 1 & 2)	3 MHz (15 PRBs)
Number of cells in network	2
Radius of each cell	2 km
Height of base-station	80 m
Height of UE	10 m
eNB transmit power (maximum)	40 dBm
$\sigma_{\text{Shadowing}}$	7 dB
Simulation time	50 TTIs
Operator 1's cost, $c_1$	0.5
Operator 2's cost, $c_2$	0.7
Secondary Access cost, $\beta$	0.3
Minimum rate per UE, $R_{j,t}^{\min}$	0.1 Mbps

# Simulation Results (2/3)

## Single User Case: One user in each OP



Average  $\alpha$  factors for OP1 and OP2 over 50 TTIs

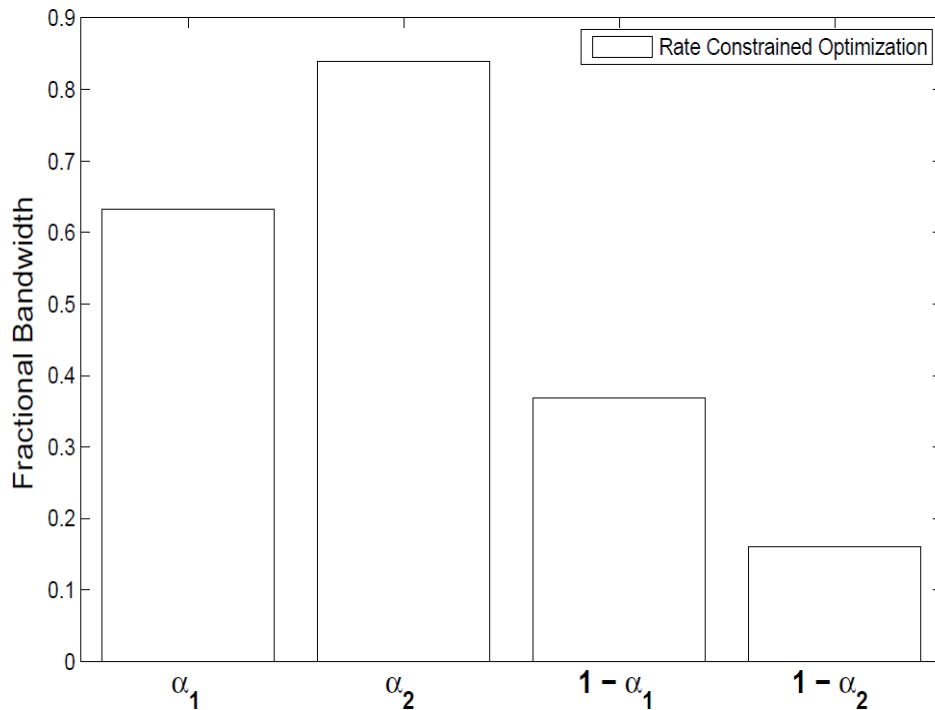


Sum Throughputs of UE1 and UE2 over 50 TTIs

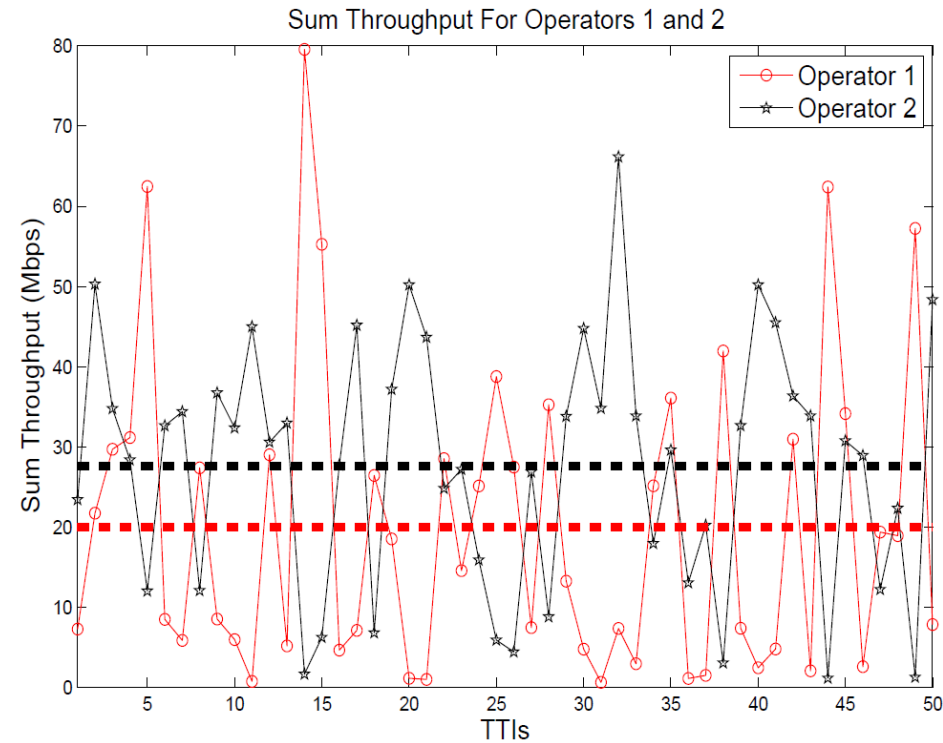


# Simulation Results (3/3)

## Multiple User Case: 2 UEs in each OP



Average  $\alpha$  factors for OP1 and OP2 over 50 TTIs



Sum Throughputs of UEs of OP1 and OP2 over 50 TTIs

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# Conclusions and Future Work

- Model for multi-operator spectrum sharing
- Solution – Weighted linear optimization
- Price of spectrum access modeled into formulation
- Trade-off of secondary spectrum cost vs. data rate investigated and mutually beneficial strategy discussed
- Extended to LTE networks
- Future Work –
  - Analyze a non-orthogonal sharing model
  - Design of power control for more efficient resource utilization
  - Optimal mode selection between orthogonal and non-orthogonal modes based on system conditions

# Thank You!

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## Questions?